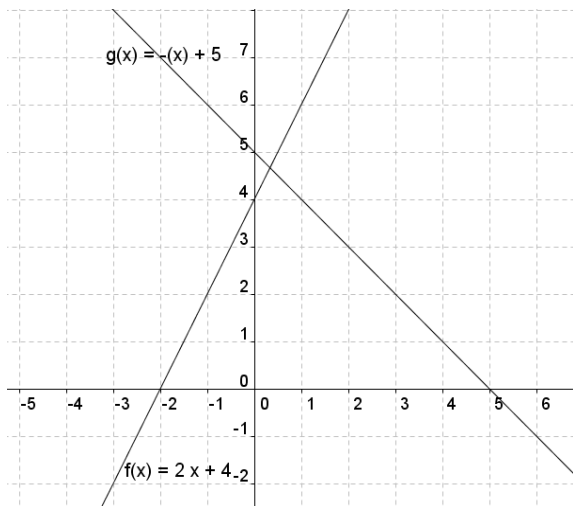


# EXAMINING FUNCTIONS WITH GEOGEBRA

GeoGebra provides many opportunities to examine a function or multiple functions simultaneously. This overview discussing some of the most used possibilities. In the official manual there is a comprehensive overview.

## Eksaminering functions

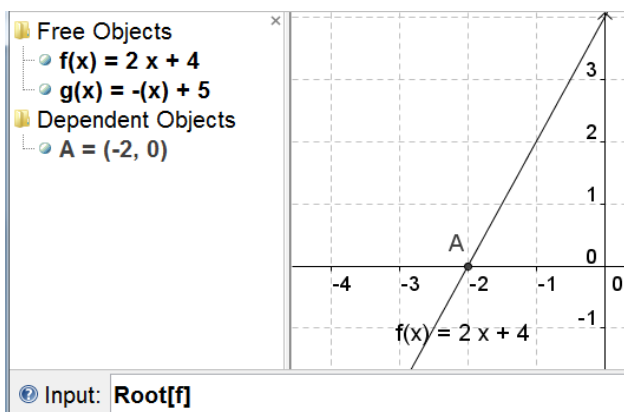
Type  $f(x) = 2x + 4$  and  $g(x) = -x + 5$  in the input bar. Adjust the axes to get this image:



We will find:

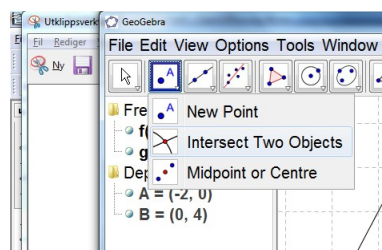
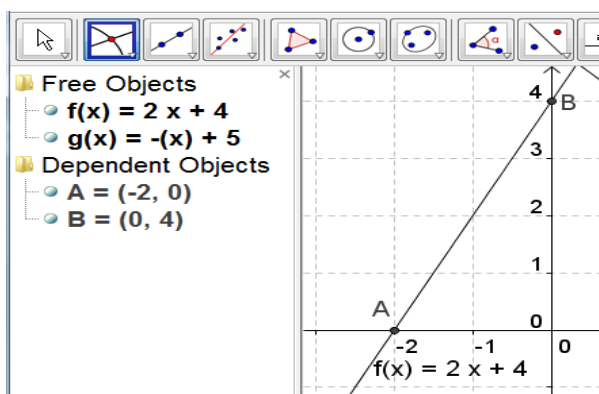
- Intersection with x-axis (roots).
- Intersection with y-axis
- Point of intersection
- A specific x-value / y-value
- Maximum/minimum (quadratic function)
- Gradient/slope (quadratic function)

## Intersection with the x-aksis (root)



Type  $\text{Root}[f]$  in the input field. GeoGebra will find the root of  $f(x)$ ,  $A = (-2, 0)$ .

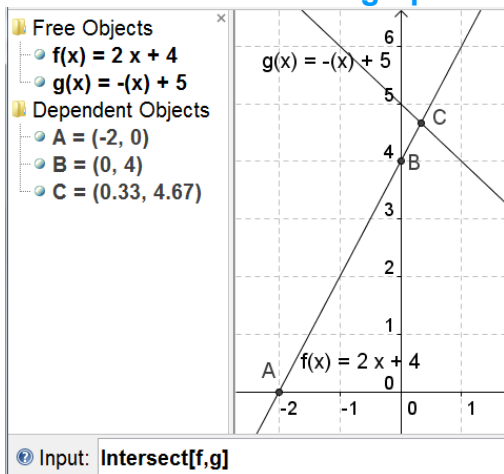
## Intersection with the y-axis



Choose **Intersect Two Objects**. Left click the x-axis, then the straight line (or reverse). GeoGebra will find  $B = (0, 4)$ .



## Intersection between graphs

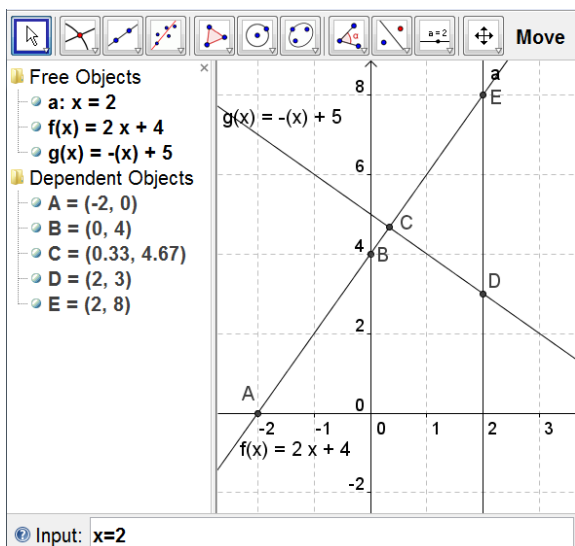


Same procedure as shown above. Alternatively use the command `Intersect[f,g]`.

GeoGebra will find the point of intersection:  
 $C = (0,33,4,67)$

## Finding the y-value when the x-value is given

Vi will find the y-value when  $x=2$



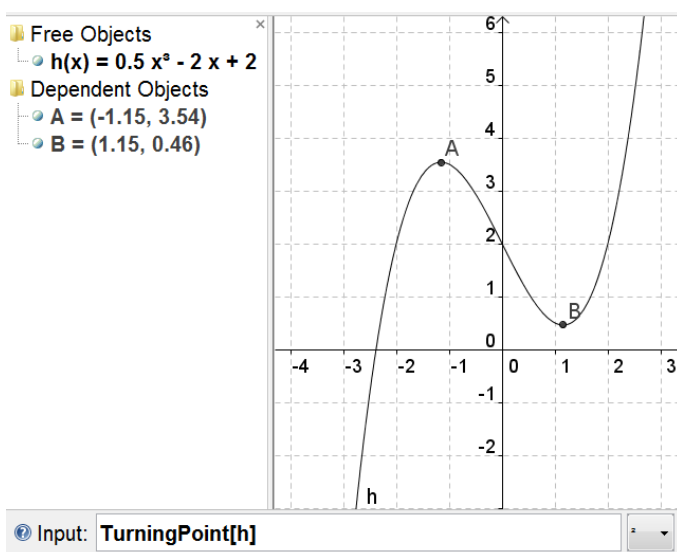
Type  $x=2$  in the input bar, and use the tool Intersect Two Objects twice (to find both intersection points). GeoGebra finds  $D = (2,3)$  between  $g$  and the line  $x=2$ , and  $E = (2,8)$  between  $f$  and the line  $x=2$ .

The desired y-values are:  $y = 3$  og  $y = 8$ .

To find x-values, we make a horizontal line instead of a vertical one. Try!

## Maximum and minimum of polynomial functions

Straight lines have no maximum or minimum. Therefore, we open a new window and draw the graph of the function  $h(x) = 0.5x^3 - 2x + 2$



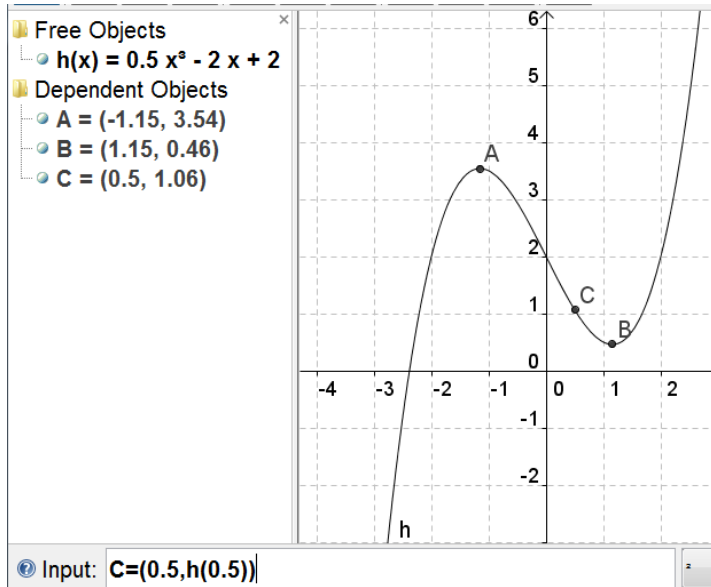
Type `TurningPoint[h]` in the input bar and press enter. GeoGebra finds maximum and minimum (if they exist). The function  $h$  have

Maximum  $A = (-1,15,3,54)$   
 Minimum  $B = (1,15,0,46)$




## Gradient / slope

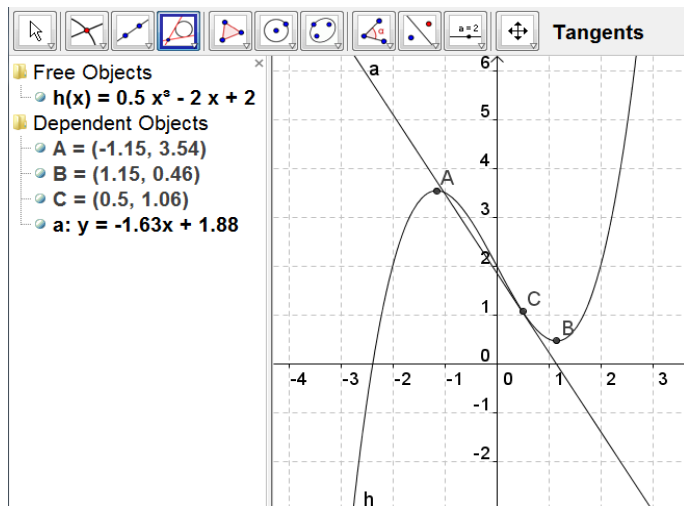
We will find the gradient of the function  $h$  when  $x = 0,5$ . First we draw a tangent line in that point. Then we find its slope.



Define the point C using the point

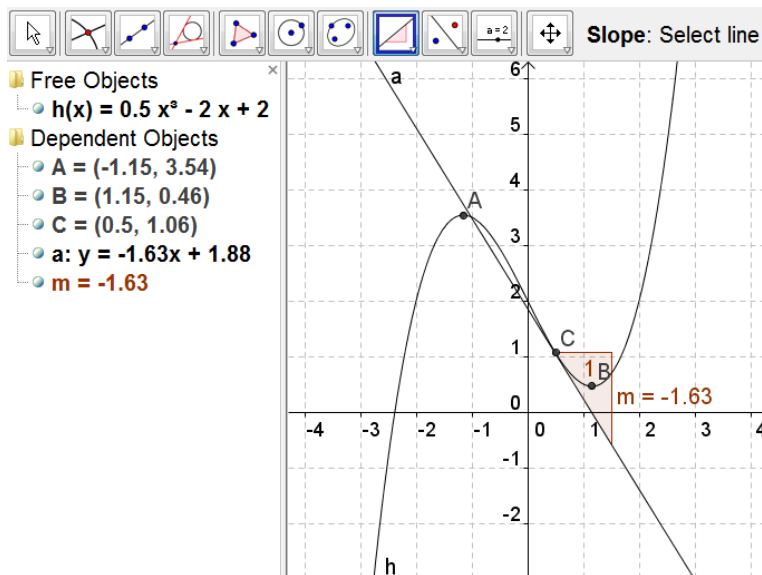
tool  or the command

$C=(0.5, h(0.5))$ .



Then we use the tool Tangents 

to draw the tangent line in C.



The tangent line is  $y = -1,63x + 1,88$

Therefore, the slope is -1,63 We can also find the slope by using the tool

slope 

The picture shows that the slope is  $m = -1,63$

